

## Defining your own “show” function

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```
data Tree a = Node a (Tree a) (Tree a)
            | Leaf a
```

```
Main> Leaf 3
ERROR: Cannot find "show" function for:
*** Expression : Leaf 3
*** Of type : Tree Integer
```

```
instance (Show a) => Show (Tree a) where
    show = showTree

showTree = ...
```

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```
data Tree a = Node (Tree a) (Tree a)
            | Leaf a
```

```
instance (Show a) => Show (Tree a) where
    show = showTree
```

```
showTree :: (Show a) => Tree a -> String
showTree (Leaf x)     = show x
showTree (Node l r) =
    "<" ++ showTree l ++ "|" ++ showTree r ++ ">"
```

```
> Node (Leaf 1) (Node (Leaf 2) (Leaf 3))
"<1|<2|3>>"
```

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## Derived Instances

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```
data Tree a = Node (Tree a) (Tree a)
            | Leaf a
            deriving (Eq, Show)
```

Constructs a “default instance” of class Show.  
Works for standard classes.

```
Main> Node (Leaf 1) (Node (Leaf 2) (Leaf 3))
Node (Leaf 1) (Node (Leaf 2) (Leaf 3))
Main> (Leaf 3) == (Leaf 4)
False
```

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## A Data type for $\lambda$ -terms

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```
data Term = V VarName
          | L VarName Term
          | A Term Term
          | I Int
          | Term :+: Term           -- addition
          | IFZ Term Term Term     -- if zero
          deriving (Show, Eq)
```

```
E ::= Id
    | \x.E
    | E1 E2
    | i
    | E1 '+' E2
    | ifzero E1 then E2 else E3
```

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## Environment-Based Evaluator

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- Previously, we see substitution-based evaluation for lambda calculus with constants
- Now we show an environment-based evaluator.

```
eval env expr = ... --compute a value
```

where an environment is a finite function from Identifiers to values.

Pseudo code:

```
eval [x=5, y=10] "x+y" = 15
```

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## LC Evaluator, 1

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```
data Term = V VarName
          | L VarName Term      --lambda
          | A Term Term        --application
          | I Int
          | Term :+: Term      -- addition
          | IFZ Term Term Term deriving (Show, Eq)
```

```
data Value = VI Int | VC (Value -> Value)
```

```
type VarName = String
-- Environment: associating values with `free' variables
type Env = [(VarName, Value)]
lookup :: Eq a => a -> [(a, b)] -> Maybe b
maybe :: b -> (a -> b) -> Maybe a -> b
maybe n f Nothing = n
maybe n f (Just x) = f x
lkup :: Env -> VarName -> Value
lkup env x = maybe err id $ lookup x env
  where err = error $ "Unbound variable " ++ x
```

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## LC Evaluator, 2

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```
data Term = V VarName
          | L VarName Term
          | A Term Term
          | I Int
          | Term :+: Term           -- addition
          | IFZ Term Term Term     deriving (Show, Eq)
```

```
data Value = VI Int | VC (Value -> Value)
```

```
type VarName = String
-- Environment: associating values with `free' variables
type Env = [(VarName, Value)]
lkup :: Env -> VarName -> Value
lkup env x = maybe err id $ lookup x env
  where err = error $ "Unbound variable " ++ x
-- Denotational semantics. Why? How to make it operational?
eval :: Env -> Term -> Value
eval env (V x) = lkup env x
...
```

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## LC Evaluator, 3

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```
data Term = ... | I Int
          | Term :+: Term           -- addition
          | IFZ Term Term Term     deriving (Show, Eq)
```

```
eval env (I n) = VI n           -- already a value
eval env (e1 :+: e2) =
  let v1 = eval env e1
      v2 = eval env e2
  in case (v1,v2) of
      (VI n1, VI n2) -> VI (n1+n2)
      vs -> error $ "Trying to add non-integers:" ++ show vs
eval env (IFZ e1 e2 e3) =
  let v1 = eval env e1
  in case v1 of
      VI 0 -> eval env e2
      VI _ -> eval env e3
      v    -> error $ "Trying to compare a non-integer
                    to 0: " ++ show v
```

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## LC Evaluator, 4

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```
data Term = ... | L VarName Term  --lambda
            | A Term Term        --app
            ... deriving (Show, Eq)
```

```
data Value = VI Int | VC (Value -> Value)
```

```
eval env (L x e) = VC (\v -> eval (ext env (x,v)) e)

ext :: Env -> (VarName,Value) -> Env
ext env xt = xt : env

eval env (A e1 e2) =
  let v1 = eval env e1
      v2 = eval env e2
  in case v1 of
      VC f -> f v2
      v    -> error $ "Trying to apply a non-function: "
                    ++ show v
```

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